MR Sim

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MR Sim is a library for simulating material removal from abrasive material removal processes. The library is built to be modular to allow different models, tool types, tool shapes, and pressure distributions to be simulated and included.

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Example 1

This example simulates a round orbital sander on a flat surface with a sinsoidal motion in the X direction. The sander is set to have orbital speed, but no rotational speed.

```
from context import mr_sim
import numpy as np
import matplotlib.pyplot as plt
R = 3.5 / 2 * 25.4 / 1000
length = 208 / 1000
period = 0.2 * 20
dt = period / 1000
dt = dt / 4
amp = length / 2
Simulation = mr_sim.create_simulation(
   mr_sim.Round, mr_sim.Flat, mr_sim.Orbital, mr_sim.Preston
simulation = Simulation(
   length + 2 * R,
   2 * R,
   kp=1.362e-9,
   radius=R,
   eccentricity=0.1875 * 25.4 / 1000,
   dt=dt,
    auto_velocity=True,
simulation.set_speed(620)
simulation.set_force(15)
for t in np.arange(0, period / 2, dt):
    simulation.set_location(amp * np.cos(2 * t * np.pi / period))
    simulation.step()
```

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plt.figure()
simulation.plot()
plt.show()

Example 2

This example simulates a purely rotary tool on a flat surface traveling on a Peano Weaving path.

```
from context import mr_sim
import numpy as np
from hilbertcurve.hilbertcurve import HilbertCurve
import matplotlib.pyplot as plt
R = 0.1
spacing = 1.75 * R
velocity = 0.1
dt = 0.05
Simulation = mr_sim.create_simulation(
   mr_sim.Round, mr_sim.Flat, mr_sim.Rotary, mr_sim.Preston
curve = HilbertCurve(3, 2)
points = np.array(
    [curve.coordinates_from_distance(d) for d in range(curve.max_h + 1)], np.float
points -= curve.max_x / 2
points *= spacing
t_final = curve.max_h * spacing / velocity
point_times = np.linspace(0, t_final, points.shape[0])
t = np.arange(0, t_final, dt)
path = np.vstack(
    (np.interp(t, point_times, points[:, 0]), np.interp(t, point_times, points[:, 1]))
) . T
size = spacing * curve.max_x + 2 * R
```

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```
simulation = Simulation(
    size, size, radius=R, dt=dt, dx=0.005, dy=0.005, auto_velocity=True
)

simulation.set_speed(100)
simulation.set_force(5)

for location in path:
    simulation.set_location(*location)
    simulation.step()

plt.figure()
simulation.plot()
plt.plot(points[:, 0], points[:, 1], ":w", linewidth=0.5)
plt.show()
```

Util

```
mr_sim.create_simulation(*classes)
```

A helper method to combine classes.

This method combines classes representing different elements of a material removal simulation. This allows different simulations to be easily constructed.

Parameters *classes – Variable length argument list of classes to subclass.

Returns A class which is a subclass of all classes provided as arguments.

Examples

For example, to use the Preston equation to simulate a round orbital sander sanding a flat surface, the following can be used.

In this example radius sets the radius of the sander defined in the Round class, eccentricity sets the eccentricity of the orbital sander defined in the Orbital class, dt sets the timestep in the Base class, which is a superclass of all other classes, and kp sets the constant in the Preston Equation class, Preston.

The same result can be accomplished manually.

This approach would be particularly useful if additional functionality needs to be added to the simulation class.

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Base

```
class mr_sim.base.Base (size\_x, size\_y, dx=0.001, dy=0.001, dt=1, auto\_velocity=False) The base simulation class.
```

This is the base simulation class. It is combined with other classes to define other attributes about the simulation.

Х

A 2D array of the X coordinates of the part with the origin at the center of the part surface.

Type numpy.ndarray

Y

A 2D array of the Y coordinates of the part with the origin at the center of the part surface.

Type numpy.ndarray

profile

A 2D array of the depth of material removed from the part surface.

Type numpy.ndarray

dt

The timestep used in the simulation.

Type float

auto_vel

If True automatically calculate the linear velocity of the tool moving over the part surface.

Type bool

x

The current X location of the center of the tool in relation to the center of the part surface.

Type float

У

The current Y location of the center of the tool in relation to the center of the part surface.

Type float

vl x

The current X direction velocity of the tool moving over the part surface.

Type float

vl_y

The current Y direction velocity of the tool moving over the part surface.

Type float

Note: Other classes must be used to include the shape and mrr methods needed by this class.

Parameters

- $size_x(float)$ The size of the part surface in the X direction.
- **size_y** (*float*) The size of the part surface in the Y direction.
- dx (float) The density of points to track in the X direction. Defaults to 0.001.
- **dy** (float) The density of points to track in the Y direction. Defaults to 0.001.
- **dt** (float) The simulation timestep. Defaults to 1.
- **auto_velocity** (bool) If True automatically calculate the linear velocity of the tool over the part surface.

local_grid()

Returns a coordinate system centered at the tool origin.

Returns The X, Y coordinate system shifted so the origin is at the center of the tool.

Return type numpy.ndarray, numpy.ndarray

```
plot (normalize=False, **kwargs)
```

Plot the simulation result.

This function uses matplotlib to plot the result of the simulation in the current figure.

Parameters

- **normalize** (bool) Normalize max depth of material removed to 1. Defaults to False.
- **kwargs Keyword arguments to be included in the call to the matplotlib. pyplot.imshow function.

Returns The AxesImage object of the plotted heatmap.

Return type matplotlib.image.AxesImage

$set_location(x=0, y=0)$

Set the current location of the center of the tool.

Sets the current location of the center of the tool with respect to the middle of the part.

Parameters

- **x** (float) The X location of the tool. Defaults to 0.
- **y** (float) The Y location of the tool. Defaults to 0.

$set_velocity(x=0, y=0)$

Sets the current linear velocity of the tool over the part surface.

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Parameters

- \mathbf{x} (float) The X velocity of the tool. Defaults to 0.
- \mathbf{y} (float) The Y velocity of the tool. Defaults to 0.

Note: If auto_velocity was set to True this method is not required.

step()

Move the simulation forward one timestep.

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Models

```
class mr_sim.models.Preston(*args, kp=1, **kwargs)
```

A class implementing the Preston Equation for material removal simulation.

This class calculates material removal rate using the Preston Equation,

$$\dot{h} = k_p p v,$$

where \dot{h} is the depth of material removed per unit time, k_p is a constant known as the Preston coefficient, p is the contact pressure between the tool and the workpiece, and v is the total speed of the tool rubbing the workpiece.

Note: This class must be subclassed by a class providing the pressure and velocity functions.

kp

The value of the Preston coefficient, k_p .

Type float

Parameters

- *args Arguments to be passed on to superclasses.
- kp(float) The Preston coefficient, k_p . Defaults to 1.
- **kwargs Keyword arguments to be passed on to superclasses.

mrr(x, y)

Calculates the material removal rate.

This function returns the material removal rate for all locations on the part surface using the Preston Equation.

x (numpy.ndarray): A 2D array of the X coordinates of the part centered at the current tool location.

y (numpy.ndarray): A 2D array of the Y coordinates of the part centered at the current tool location.

Returns The material removal rate at all locations on the part surface.

Return type numpy.ndarray

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Pressure Distributions

```
class mr_sim.pressure.Flat(*args, **kwargs)
```

A class used to calculate the pressure applied to a flat surface.

This class determines the pressure applied to a flat surface from the normal force and torques applied to the tool.

Note: This class assumes that all points of the tool are in contact with the part surface at all time.

force

The normal force applied to the tool.

Type float

torque_x

The torque about the X axis applied to the tool.

Type float

torque_y

The torque about the Y axis applied to the tool.

Type float

Note: This class requires area, Ix, and Iy to be set by a subclass.

Parameters

- *args Arguments to be passed on to superclasses.
- ****kwargs** Keyword arguments to be passed on to superclasses.

pressure(x, y)

Determine the pressure the tool applied to the part surface.

This function calculates the pressure applied at all points on the part surface.

Parameters

- x (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- y (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array of the pressure applied by the tool.

Return type numpy.ndarray

set_force (force)

Set the current normal force applied to the tool.

Parameters force (float) – The current normal force.

$set_torque(x=0, y=0)$

Set the current torques applied to the tool.

Parameters

- **x** (float) The current torque about the X axis. Defaults to 0.
- **y** (float) The current torque about the Y axis. Defaults to 0.

```
class mr_sim.pressure.ConstantCurvature(*args, kx=0, ky=0, stiffness=None, dx=0.001, dy=0.001, **kwargs)
```

A class used to calculate the pressure applied to a surface with constant curvature.

This class determines the pressure applied to the surface from the normal force.

Note: This class models the contact pressure as a paraboloid with the specified curvature at the tool origin.

force

The normal force applied to the tool.

Type float

kx

The curvature in the x direction.

Type float

ky

The curvature in the y direction.

Type float

dx

The x direction spacing of the grid.

Type float

dy

The y direction spacing of the grid.

Type float

stiffness

The stiffness of the tool. This can be found as the Young's modulus of the tool divided by its thickness.

Type float

Parameters

- *args Arguments to be passed on to superclasses.
- **kx** (*float*) The curvature in the x direction. Defaults to 0.
- **ky** (float) The curvature in the y direction. Defaults to 0.
- **stiffness** (*float*) The stiffness of the sanding tool. Defaults to None. This can be found as the Young's modulus of the tool divided by its thickness.
- dx (float) The x direction spacing of the grid. Defaults to 0.001.
- **dy** (float) The y direction spacing of the grid. Defaults to 0.001.
- **kwargs Keyword arguments to be passed on to superclasses.

Raises ValueError - If stiffness is None.

pressure(x, y)

Determine the pressure the tool applied to the part surface.

This function calculates the pressure applied at all points on the part surface.

Parameters

- **x** (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- **y** (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array of the pressure applied by the tool.

Return type numpy.ndarray

Note: This function uses closed form solutions if the shape is *Round*, otherwise it uses scipy. optimize.minimize_scalar() which is slow.

$set_curvature(kx=0, ky=0)$

Set the curvature of the surface.

Parameters

- \mathbf{kx} (float) The curvature in the x direction. Defaults to 0.
- **ky** (float) The curvature in the y direction. Defaults to 0.

set_force (force)

Set the current normal force applied to the tool.

Parameters force (float) – The current normal force.

Tool Shapes

```
class mr_sim.shapes.Round(*args, radius=None, **kwargs)
```

A class representing a round tool for material removal simulations.

This class represents a round tool and calculates the section of the part surface which the tool is in contact with.

r

The tool radius.

Type float

area

The area of the tool.

Type float

Ιx

The second moment of area of the tool in the X direction.

Type float

Ιy

The second moment of area of the tool in the Y direction.

Type float

Note: The class attributes are set automatically when the class is initialized, and when the tool radius is set using the radius property. Setting these values manually could lead to simulation errors.

Parameters

- *args Arguments to be passed on to superclasses.
- radius (float) The radius of the tool. Defaults to None.
- **kwargs Keyword arguments to be passed on to superclasses.

Raises ValueError - If radius is not set.

radius

Tool radius.

Type float

shape (x, y)

This function finds the section of the part the tool is in contact with.

Parameters

- x (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- y (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array where True indicates the tool is in contact with that portion of the part surface.

Return type numpy.ndarray

class mr_sim.shapes.Rectangular(*args, width=None, height=None, **kwargs)

A class representing a rectangular tool for material removal simulations.

This class represents a rectangular tool and calculates the section of the part surface which the tool is in contact with.

width

The tool width, in the X direction.

Type float

height

The tool height, in the Y direction.

Type float

area

The area of the tool.

Type float

Ιx

The second moment of area of the tool in the X direction.

Type float

Ιy

The second moment of area of the tool in the Y direction.

Type float

Note: The class attributes are set automatically when the class is initialized, and when the tool size is set using the set_size method. Setting these values manually could lead to simulation errors.

Parameters

- *args Arguments to be passed on to superclasses.
- width (float) The width of the tool, in the X direction. Defaults to None.

- height (float) The height of the tool, in the Y direction. Defaults to None.
- **kwargs Keyword arguments to be passed on to superclasses.

Raises ValueError - If width or height is not set.

set_size (width, height)

Set the size of the tool.

Parameters

- width (float) The width of the tool, in the X direction.
- height (float) The height of the tool, in the Y direction.

shape(x, y)

This function finds the section of the part the tool is in contact with.

Parameters

- **x** (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- y (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array where True indicates the tool is in contact with that portion of the part surface.

Return type numpy.ndarray

```
class mr_sim.shapes.Square(*args, width=None, **kwargs)
```

A class representing a square tool for material removal simulations.

This class represents a square tool and calculates the section of the part surface which the tool is in contact with.

Note: This class simply inherits Rectangular and sets both width and height to the same value.

Parameters

- *args Arguments to be passed on to superclasses.
- width (float) The width of the tool. Defaults to None.
- ****kwargs** Keyword arguments to be passed on to superclasses.

Raises ValueError - If width is not set.

$\mathtt{set_size}\left(width\right)$

Set the size of the tool.

Parameters width (float) – The width of the tool.

Tool Types

```
class mr_sim.types.Orbital(*args, eccentricity=None, **kwargs)
```

A class for simulating a random orbit sander.

This class includes the necessary methods for calculating the total velocity of a random orbit sander.

eccentricity

The eccentric distance of the sander.

Type float

orbital_speed

The current rotational speed of the eccentric link.

Type float

rotational_speed

The current rotational speed of the pad with with respect to the part surface.

Type float

Parameters

- *args Arguments to be passed on to superclasses.
- eccentricity (float) The eccentric distance of the sander. Defaults to None.
- **kwargs Keyword arguments to be passed on to superclasses.

Raises ValueError - If eccentricity is not set.

set_speed (orbital_speed=0, rotational_speed=0)

Sets the orbital and rotational speed.

Parameters

• **orbital_speed** (float) – The current rotational speed of the eccentric link. Defaults to 0.

• rotational_speed (float) - The current rotational speed of the pad with with respect to the part surface. Defaults to 0.

velocity(x, y)

Determines the velocity of the tool

Determines the total velocity of the tool with respect to the part sufrace.

Note: This is an approximation that should be more rigerously verified.

Parameters

- x (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- y (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array of velocity on the part surface.

Return type numpy.ndarray

```
class mr_sim.types.Belt(*args, **kwargs)
```

A class for simulating a belt sander.

This class includes the necessary methods for calculating the total velocity of a belt sander.

speed

The current speed of the belt.

Type float

Parameters

- *args Arguments to be passed on to superclasses.
- **kwargs Keyword arguments to be passed on to superclasses.

set_speed(speed)

Sets the speed of the belt.

Parameters speed (float) – The current speed of the belt.

velocity(x, y)

Determines the velocity of the tool

Determines the total velocity of the tool with respect to the part sufrace.

Note: This is an approximation that should be more rigerously verified.

Parameters

- x (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- **y** (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array of velocity on the part surface.

Return type numpy.ndarray

```
class mr_sim.types.Rotary(*args, **kwargs)
```

A class for simulating a rotary abrasive tool.

This class includes the necessary methods for calculating the total velocity of a rotary tool.

speed

The current rotational speed of the tool.

Type float

Parameters

- *args Arguments to be passed on to superclasses.
- **kwargs Keyword arguments to be passed on to superclasses.

set_speed(speed)

Sets the rotational speed of the tool.

Parameters speed (float) – The current rotational speed of the tool.

velocity(x, y)

Determines the velocity of the tool

Determines the total velocity of the tool with respect to the part sufrace.

Note: This is an approximation that should be more rigerously verified.

Parameters

- **x** (numpy.ndarray) A 2D array of the X coordinates of the part centered at the current tool location.
- y (numpy.ndarray) A 2D array of the Y coordinates of the part centered at the current tool location.

Returns A 2D array of velocity on the part surface.

Return type numpy.ndarray

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